Recent progress in the topology of simplicial complexes

This talk surveys recent results in the combinatorial topology of simplicial complexes, focusing on the topics of algebraic shifting and spectra of combinatorial Laplace operators.

It turns out that these results draw attention to an unlikely heroine: the shifted simplicial complex. We attempt to build a case for studying these objects more closely.